

# Species interactions are internally constrained despite large climatic variability

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KEYWORDS: constraints, competition, variability, structural stability

SUBMITTED TO ECOLOGY AS AN ARTICLE

NUMBER OF WORDS: abstract 282, main text 3339

NUMBER OF REFERENCES: 51 references

NUMBER OF FIGURES: 4

**Open Research Statement:** Data and code needed to reproduce the results of this study are stored in a public repository: <https://figshare.com/s/e4422e607ebde18ce2a5>

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## 1 Abstract

2 Understanding how vital rates and species interactions vary over time is crucial for predicting  
3 community responses to environmental change. Considerable progress has been made in  
4 understanding the drivers of variation in vital rates. However, the question of whether interactions  
5 are highly plastic and context-dependent, or strongly constrained by internal (e.g., species traits  
6 and composition) and/or external factors (e.g., environmental conditions) remains unclear. We  
7 applied a theoretical approach based on the feasibility domain —the range of conditions allowing  
8 coexistence— to a nine-year dataset of time-changing interactions between annual plants under  
9 large variability in annual precipitation. Using subcommunities of three species, we found that  
10 species interactions are strongly constrained, forming a “core-periphery” structure of consistently  
11 feasible combinations across years. This main finding means that species sample repeatedly a  
12 restricted range of opportunities for coexistence. Similar findings were obtained for subcommunities  
13 of four species. Crucially, the constraints to variation in biotic interactions are determined by  
14 species identity (internal constraints) rather than precipitation or temporal autocorrelation  
15 (external environmental factors). Furthermore, we found a contrasting effect of precipitation on the  
16 feasibility of subcommunities. While wetter years increase similarity between subcommunities and  
17 reduce the overall feasible range, drier years increase dissimilarity between subcommunities and  
18 increase the probability of coexistence when the conditions seem harsher. These findings suggest  
19 that constraints to biotic interactions tend to be alike across species in wetter years, but more  
20 context dependency occurs across species in drier years. Our findings challenge the assumption of  
21 highly plastic species interactions even in a highly dynamic system of annual plants. Our results  
22 also highlight the critical importance of internal constraints generated by species identity in  
23 mediating community persistence and predicting community responses to environmental change.

## 24 Introduction

25 To predict how ecological communities will respond to a changing world, we need to  
26 understand two intertwined processes: the vital rates of individual species [Bernhardt  
27 et al., 2020, Boyce et al., 2006], and the complex web of interactions between them  
28 [Brooker, 2006, Tylianakis et al., 2008]. Organisms of the same species share characteristic  
29 traits like body size, feeding strategy, or metabolic rates that produce vital rates (survival,  
30 growth, and reproduction) that differ between species [Adler et al., 2014]. Analogously, the  
31 characteristic traits of a species determine how often it interacts with other species, the  
32 kind of interaction, how strong these interactions are, and how symmetric [Pérez-Ramos  
33 et al., 2019, Strydom et al., 2021]. Together, these two components determine population  
34 dynamics while also potentially providing species with flexibility to cope with novel  
35 fast-changing environments. While considerable progress has been made in understanding  
36 the responses of individual species vital rates [Compagnoni et al., 2021, Slein et al., 2023],  
37 a critical piece of the puzzle remains missing. Whether and how these interactions  
38 themselves —the architects of ecosystem stability— shift and reorganize in response to  
39 environmental variability remains largely unknown. Obtaining this information is critical  
40 to understand how much environmental variation a community can withstand before losing  
41 species [Grilli et al., 2017], since species interactions determine what combinations of vital  
42 rates allow for the persistence of all species in the community [Saavedra et al., 2017].  
43 Species interactions, as a measure of the effect of one species on the growth rate of another,  
44 are not fixed. Their strength (weak vs. strong) and sign (positive vs. negative) vary  
45 markedly across space and time [CaraDonna et al., 2017, Ushio et al., 2018, Zvereva and  
46 Kozlov, 2021]. Although some species traits or abiotic conditions seem to generate some

47 patterns [Daniel et al., 2024, Maestre and Cortina, 2004], the prevailing view holds that  
48 most changes in species interactions are highly context-dependent and hence difficult to  
49 predict [Catford et al., 2022, Chamberlain et al., 2014, Song et al., 2020]. This inherent  
50 variability and unpredictability raise a fundamental question: Are changes in species  
51 interactions essentially random, or are they constrained by underlying factors? These  
52 constraints could arise from either internal community characteristics such as species  
53 identity with their particular trait profile and evolutionary origin, or from external  
54 environmental drivers such as rainfall variability. Understanding the nature and strength of  
55 these constraints is essential for predicting how ecological communities will respond to  
56 ongoing environmental change and to develop effective conservation strategies [Tylianakis  
57 et al., 2008].

58 To address the dichotomy of the internal versus external forces shaping species  
59 interactions, we adopt a structuralist approach [Saavedra et al., 2017, Svirezhev and  
60 Logofet, 1978] that allows scaling up from prior pairwise approaches [Hallett et al., 2019,  
61 Kraft et al., 2015a] to consider a community-level perspective. Within this approach, a key  
62 concept is the feasibility domain, which allows quantifying the various constraints on  
63 species interactions. As an analogy, think of the feasibility domain as a “safe operating  
64 space” for the community: it represents the range of conditions —such as combinations of  
65 growth rates— where all species can coexist [Godoy et al., 2018, Saavedra et al., 2017]. A  
66 larger and more symmetric feasibility domain implies a higher probability of long-term  
67 community persistence [Allen-Perkins et al., 2023, Song et al., 2018]. While this framework  
68 has typically been used to analyze communities with fixed interactions [Saavedra et al.,  
69 2017], we extend it to a dynamic system with changing interactions: how the feasibility

70 domain —a direct reflection of the current interaction network— itself moves and morphs  
71 in response to environmental change [Song et al., 2018, 2020].

72 The dynamic feasibility domain approach allows us to describe how the feasibility domains  
73 of different years explore the range of possible parameters — growth rates in this case —  
74 and if their movements between consecutive years are gradual or abrupt. Using this  
75 technique, we can test three distinct hypotheses about the nature of constraints on species  
76 interactions (Figure 1). First, strong internal constraints may dictate interactions, driven  
77 primarily by fixed species traits (e.g., phenology, functional traits) [Daniel et al., 2024,  
78 Olesen et al., 2011] or taxonomic identity [Godoy et al., 2014]. If this is the case, feasibility  
79 domains from different years would consistently overlap, forming a *core-periphery structure*,  
80 where a central region of the interaction space is consistently feasible (Figure 1 a). Second,  
81 multiple external constraints could drive shifts between distinct states of species  
82 interactions. For example, alternating periods of drought and flooding might lead to  
83 different community configurations or changes in relative abundances [Fujita et al., 2023]  
84 and, consequently, feasibility domains using distinct areas of the parameter space (Figure 1  
85 b). Third, a lack of strong constraints might result in feasibility domains that vary  
86 randomly across the parameter space, reflecting a high degree of environmental forcing or  
87 stochasticity (e.g., strong effect of precipitation or dispersion) in community assembly  
88 (Figure 1 c). As each scenario provides different distributions of overlaps between feasibility  
89 domains of consecutive years (Figure 1 d-f), our theoretical framework provides a powerful  
90 method to distinguish between internal and external constraints on species interactions.

91 With our approach, we hypothesize that if internal constraints are dominant, randomizing  
92 species identities within the interaction matrix should disrupt the core-periphery pattern

93 and the observed temporal conservation of the feasibility domain. In contrast, external  
94 constraints creating a similar *core-periphery structure* act through autocorrelation in  
95 environmental conditions or by species-mediated modifications of the microenvironment.  
96 For instance, species can gradually build up thick litter layers (e.g., grasses with litter hard  
97 to decompose) or increase the abundance of natural enemies that persist in the soil (e.g.,  
98 forbs with large and soft leaves that are attacked by fungi) [Bever, 2003, Bever et al.,  
99 2015]. If these externally driven, time-dependent processes are the main constraint, then  
100 the order in which species interactions occur over time becomes crucial. Specifically,  
101 interaction matrices from consecutive years should be more similar than those from more  
102 distant years. Therefore, randomizing the temporal order of these matrices should  
103 eliminate this time-dependent similarity (temporal autocorrelation) and allow an  
104 assessment of origin of the constraints.  
105 We test these hypotheses using a unique, nine-year dataset of temporal variation in species  
106 interactions in a Mediterranean grassland community (Doñana National Park, Spain). This  
107 system is characterized by annual plants from diverse taxonomic groups, experiencing  
108 highly variable annual precipitation (Appendix S1: Figure S4), making it an ideal system  
109 for investigating to what extent internal constraints versus environmental variability shape  
110 species interactions. By integrating detailed field observations with our structuralist  
111 approach, we provide the first empirical assessment of the constraints governing species  
112 interaction variation in a multi-species natural community.

## 113 Methods

### 114 Study system

115 We collected data from our field site in Caracoles Ranch, a natural grassland with no cattle  
116 present, located within Doñana National Park (SW Spain 37.07° N, 6.31° W). The area has  
117 a Mediterranean climate with a mean temperature of 17.5° C and a mean precipitation of  
118 460 mm for the period 2000-2023. A small slope generates a gradient of soil salinity and  
119 humidity. Vegetation on this site is dominated by annual plant species, with perennial  
120 species barely present.

121 In September 2014, we established nine plots of 8.5 m x 8.5 m along this environmental  
122 gradient, divided into three blocks of three. Plots were separated by an average distance of  
123 30 m (minimum 20 m) and blocks by an average distance of 300 m. Each plot was divided  
124 into 36 subplots of 1 x 1 m with corridors of 0.5 m in between to allow access for  
125 measurements. For nine growing seasons (2015-2023), we measured abundances of every  
126 species in every subplot. We used nine interaction matrices (one per year), previously  
127 estimated from these field observations following a methodology already used and tested  
128 [García-Callejas et al., 2021], for the seven most common species that were present every  
129 year in every plot (Appendix S1: Table S1). These matrices characterize the interaction  
130 structure of this community every year by including the per capita effects of each species  
131 on itself and on all other species.

### 132 Feasibility domains and overlap

133 Our approach was to use mainly subcommunities of triplets of species as our unit of  
134 analysis, giving a total of 35 combinations of species, although we also extended our

135 evaluation's main findings to subcommunities of four species (Appendix S1: Figure S3).

136 We chose these levels of richness because, while offering some of the complexity of  
137 multispecies systems beyond simple pairs, they produce feasibility domains big enough to  
138 create patterns of overlap and, in addition, the three species case can be graphically  
139 represented in two dimensions for an easier interpretation. Note that this approach works  
140 for combinations of three and four species from the total of seven species with available  
141 interactions data. But, as the size of the feasibility domain depends on the number of  
142 species [Dougoud et al., 2018], we cannot approach each subcommunity to the total  
143 number of species because feasibility domains tend to become smaller and the overlap  
144 patterns eventually disappear. For those particular cases, the alternative would be to  
145 measure the distance between centroids or the nearest sides of consecutive feasibility  
146 domains. We calculated the feasibility domain for each combination of subcommunity and  
147 year from the corresponding matrix of interactions. Assuming that the population  
148 dynamics in a community can be approximated by a Lotka-Volterra system, we define as  
149 feasible equilibria of that system those where all species have positive abundances. The  
150 region of the parameter space of intrinsic growth rates that leads to feasible equilibria  
151 given an interaction matrix is known as the feasibility domain [Saavedra et al., 2017, Song  
152 et al., 2018]. We calculated the size of the feasibility domain as the normalized solid angle  
153  $\Omega(A)$  that is equal to the probability of sampling uniformly a vector of intrinsic growth  
154 rates on the unit sphere inside the feasibility domain [Song et al., 2018]. The normalized  
155 solid angle  $\Omega(A)$  can be defined as

$$\Omega(A) = \frac{\text{vol}(D_F(A) \cap \mathbb{B}^S)}{\text{vol}(\mathbb{B}^S)} \quad (1)$$

156 where  $\mathbb{B}^S$  is the closed unit ball in dimension S. We calculated the overlap between pairs of  
157 feasibility domains as the shared normalized solid angle  $\Omega(A \cap B)$  [Song et al., 2018], that  
158 is the range of conditions under which the community is feasible under both matrices. We  
159 calculated the overlap between pairs in three different scenarios:

- 160 1. Overlaps between feasibility domains of observed matrices in the observed order.
- 161 2. Overlaps between feasibility domains of matrices with their elements randomized in  
162 the observed order.
- 163 3. Overlaps between feasibility domains of observed matrices in a randomized order.

164 In our analytical design, to numerically estimate the differences in mean overlap between  
165 different scenarios with triplets, we applied a multi-membership mixed model for repeated  
166 measures to the overlap data. In that model, we incorporated the differences in mean  
167 overlap created by species identity nested in our subcommunities, since different  
168 subcommunities are not fully independent from each other, but rather they share species.

169 We did it by implementing a presence/absence matrix of species in each observation (mean  
170 accumulated overlap for a triplet and 2-9 years) as a random factor.

## 171 Environmental effects

172 To examine the effect of environmental variability, we also compiled precipitation data  
173 from the nearest meteorological station for the years 2015-2023 in the form of mm of  
174 precipitation per hydrological year (September - August) (Appendix S1: Figure S4,  
175 Estación Meteorológica de Aznalcázar, Junta de Andalucía). For this analysis, we  
176 calculated similarity between matrices of all subcommunities in every year as the inverse of  
177 the Euclidean distance calculated as

$$d(A, B) = \sqrt{\sum_{i=1}^n \sum_{j=1}^n (a_{ij} - b_{ij})^2} \quad (2)$$

178 where the distance between two matrices  $(A, B)$  is estimated as the square root of the sum  
179 of the squares of the differences between elements  $a_{ij}$  and  $b_{ij}$  for every position  $ij$ . We also  
180 calculated mean size ( $\Omega$ ) of the feasibility domains in every year, and then we compared  
181 these variables against precipitation of the corresponding hydrological year (September -  
182 August). For each variable, we calculated the slope of the linear regression against  
183 precipitation with a 95% confidence interval and Spearman's correlation.  
184 All analyses and figures were implemented using R v4.5.0 [R Core Team, 2024] and  
185 packages *tidyverse* [Wickham et al., 2019], *feasoverlap* [Song et al., 2018], *gtern* [Hamilton  
186 and Ferry, 2018], *lme4* [Bates et al., 2015], and *proxy* [Meyer and Buchta, 2022].

## 187 Results

188 We found that species interactions are highly structured across the nine years. Rather than  
189 exhibiting random variation, we found strong evidence for internal constraints shaping the  
190 dynamics of these interactions. The feasibility domains, representing all feasible  
191 combinations of intrinsic growth rates for the case of three-species subcommunities, were  
192 not randomly distributed across the parameter space. Instead, we observed a distinct  
193 core-periphery structure (Figure 2, Appendix S1: Figure S1): certain regions of the  
194 parameter space are consistently feasible across years, forming a “core”, while other regions  
195 are only transiently feasible, constituting the “periphery”. This finding is *a priori*  
196 surprising for a strong dynamical system such as ours, where annual plant species complete

197 their entire life cycle within a single year, and the community studied experiences strong  
198 interannual environmental variation. Thus, this persistence of the core-periphery structure  
199 strongly suggests underlying constraints that operate despite these dynamic forces.

200 To differentiate between internal and external constraints, we compared the overlap of  
201 feasibility domains between consecutive years in three scenarios: the *observed* time series,  
202 *randomized* time series (with interaction coefficients shuffled within matrices), and  
203 *disordered* time series (with the temporal order of matrices randomized) (Figure 3). This  
204 comparison rigorously accounted for repeated measurements through time and the  
205 non-independence of subcommunities (see Methods). Our results demonstrate that the  
206 degree of overlap in the observed time series significantly exceeded that of both the  
207 randomized and disordered scenarios (Figure 3 a). Notably, the largest difference was  
208 observed between the observed and randomized-interactions scenarios, with only a slight  
209 difference between the observed and disordered-time-series scenarios. These results  
210 strongly suggest that, in this system, internal constraints are the primary drivers of the  
211 core-periphery structure, with a smaller contribution from temporal autocorrelation in the  
212 structure of species interactions.

213 Given the dominance of internal constraints, a remaining question is what role the  
214 environmental variability plays in our study system. We found that annual precipitation, a  
215 known driver of community dynamics in this system [Godoy et al., 2024], exerts a complex  
216 influence on the feasibility domains. Years with higher precipitation are associated with a  
217 significant reduction in the average size ( $\Omega$ ) of the feasibility domains across  
218 subcommunities (Figure 4 a). Simultaneously, however, the feasibility domains themselves  
219 become more similar between them in wetter years (Figure 4 b). The combination of these

220 last two findings suggests that the wetter the conditions, the more constrained the  
221 interactions across all triplets of species to the same narrow part of the parameter space, so  
222 all subcommunities need similar conditions to coexist. Conversely, these results also  
223 suggest that two mechanisms increase the opportunities for species to coexist when the  
224 conditions are drier. First, the feasibility domain for each subcommunity tends to be  
225 bigger, and second, the feasibility domains of different subcommunities are positioned at  
226 different locations of the parameter space, which overall increases the likelihood of the  
227 system to maintain diversity by covering a larger fraction of the parameter space.

## 228 Discussion

229 It is widely acknowledged that species interactions are fundamental to maintaining  
230 biodiversity, yet our understanding of the temporal dynamics of these interactions remains  
231 surprisingly limited and not connected to how stable communities are against  
232 environmental variation. Part of this limitation is because much of the recent debate has  
233 centered on whether these changes are deterministic or stochastic [CaraDonna et al., 2017,  
234 Catford et al., 2022, Chamberlain et al., 2014, Daniel et al., 2024, Hallett et al., 2019,  
235 Ushio et al., 2018]. However, this focus often overlooks a more fundamental question: To  
236 what extent are species interactions constrained, as opposed to being highly plastic and  
237 adaptable? Our findings strongly support the view that interactions are constrained by the  
238 composition of species within communities, while external drivers such as precipitation  
239 —commonly believed to play a major role [Hallett et al., 2019, Matías et al., 2018,  
240 Van Dyke et al., 2022, Wainwright et al., 2019]— have a comparatively minor effect on  
241 generating variation in interactions. Additionally, we found evidence that our communities

242 show a temporally auto-correlated structure. This finding is surprising in a community of  
243 annual plants, indicating that the system retains a “memory” of past interactions and  
244 abundances that influences short-term dynamics. While the underlying mechanisms are not  
245 yet fully understood, we hypothesize that this temporal autocorrelation could reflect  
246 gradual changes in species abundances or small-scale habitat modifications such as  
247 attracting natural enemies [Song et al., 2021] and self-limiting processes such as litter  
248 build-up [Letts et al., 2015].

249 The observed constraints on species interactions have significant implications for  
250 understanding the maintenance of species diversity, particularly given the increasing  
251 environmental variability driven by human activities. Our finding that these constraints  
252 are strong and internally driven suggests that communities have a limited capacity to  
253 absorb environmental change before species extinctions occur [Saavedra et al., 2017, Song  
254 et al., 2020]. Specifically, stronger constraints mean a smaller portion of the feasibility  
255 domain is accessible, increasing the likelihood that environmental fluctuations will push the  
256 intrinsic growth rates of the system outside the bounds of species positive growth rates,  
257 which can negatively impact biodiversity because species can no longer thrive in the system  
258 [Allen-Perkins et al., 2023, Grilli et al., 2017]. Consequently, even seemingly minor  
259 environmental shifts can trigger substantial changes in community composition [Van Dyke  
260 et al., 2022]. Therefore, the maintenance of biodiversity under such changing conditions  
261 relies heavily on compositional shifts: different species assemblages occupying distinct  
262 regions of the parameter space (see Appendix S1: Figure S1). This perspective offers a  
263 crucial complement to existing explanations for the widely documented pattern of species  
264 turnover across broad temporal and spatial climatic gradients [Buckley and Jetz, 2008,

265 Korhonen et al., 2010]. While it is well-established that species adapt to local conditions  
266 —a process where the environment effectively filters the community members  
267 [HilleRisLambers et al., 2012, Kraft et al., 2015b]— our findings highlight that the inherent  
268 constraints on how species can interact within the available species pool are equally  
269 important in determining which species combinations are viable.

270 A key conclusion from our study is that the strength and sign of species interactions within  
271 ecological communities does not follow a completely random structure. In other words,  
272 species interactions are demonstrably constrained by biological factors, meaning that  
273 communities explore only a limited portion of the theoretically available feasibility domain.  
274 This finding has important implications for theoretical ecology, particularly for a large and  
275 influential body of work that uses network approaches based on random matrices to study  
276 species coexistence in species-rich communities [Akjouj et al., 2024, Allesina and Tang,  
277 2012, Gibbs et al., 2022, May, 1972]. These models assume that species interactions are  
278 assigned randomly —that is, species interact with a given probability and with a strength  
279 drawn from a statistical distribution—. While we fully acknowledge the significant  
280 contributions of this random-matrix approach, our results suggest that its direct  
281 applicability to real-world communities may be limited by its inherent assumption of  
282 random interactions. A more realistic and potentially fruitful direction for future  
283 theoretical work could involve incorporating internal constraints on interactions in these  
284 network models. That is, combining a probabilistic approach [Strydom et al., 2021] with  
285 the creation of species “identities”, a set of constraints that define how often a species  
286 interacts with other species, the kind of interactions, how strong these interactions are, and  
287 how symmetric.

288 An intriguing finding of our study is that environmental variation in the form of  
289 precipitation variability does not have uniform effects on different facets of species  
290 interactions and feasibility. Specifically, the drier and wetter ends of the annual  
291 precipitation gradient have contrasting impacts. While drier years allow subcommunities to  
292 explore different subsections of the parameter space that are bigger in average, wetter years  
293 reduce this variation, making all subcommunities behave more alike and making their  
294 feasibility domains shrink in average. From our experience observing the study system  
295 during a decade, we deduce that these patterns emerge because in drier years competition  
296 is relaxed and may even shift to facilitation as total biomass remains low, while in wetter  
297 years, total biomass is way higher and there are enough plants and of a big enough size as  
298 to compete for resources like nutrients and light. The ecological meaning is that drier years  
299 increase the opportunities for coexistence, while the opposite is true in wetter years. These  
300 temporal processes affecting the feasibility of natural communities have never been  
301 reported before beyond our study system, and they imply that the directionality of the  
302 environmental change matters for constraining interactions and maintaining diversity.

303 In conclusion, our study demonstrates that even in a highly dynamic system of short-lived  
304 annual plants, species interactions are strongly constrained, primarily by the identity of the  
305 interacting species. It is reasonable to hypothesize that longer-lived organisms, such as  
306 perennial plants or trees, might exhibit even stronger constraints due to their slower  
307 growing strategies, though this requires further validation. Our study has therefore  
308 implications for how the local species pool can cope with changing environmental  
309 conditions, and makes complementary explanations for changes in species composition  
310 across broad environmental gradients. Taken together, these results underscore the critical

311 need to incorporate the constrained nature of species interaction variability into both our  
312 understanding and our predictions of species coexistence and biodiversity maintenance.

313 **Acknowledgements:** SP acknowledges financial support provided by the University of  
314 Cádiz (UCA/R93REC/2019). OG acknowledges financial support provided by the Spanish  
315 Ministry of Economy and Competitiveness (MINECO) and by the European Social Fund  
316 through TASTE (PID2021-127607OB-I00) project.

317 **Author Contributions:** SP, CS, and OG conceptualized the idea, SP and CS conducted  
318 main statistical analyses, SP wrote the first version of the manuscript, CS and OG  
319 contributed significantly to editing and revision.

320 **Conflict of Interest Statement:** The authors declare no conflict of interest.

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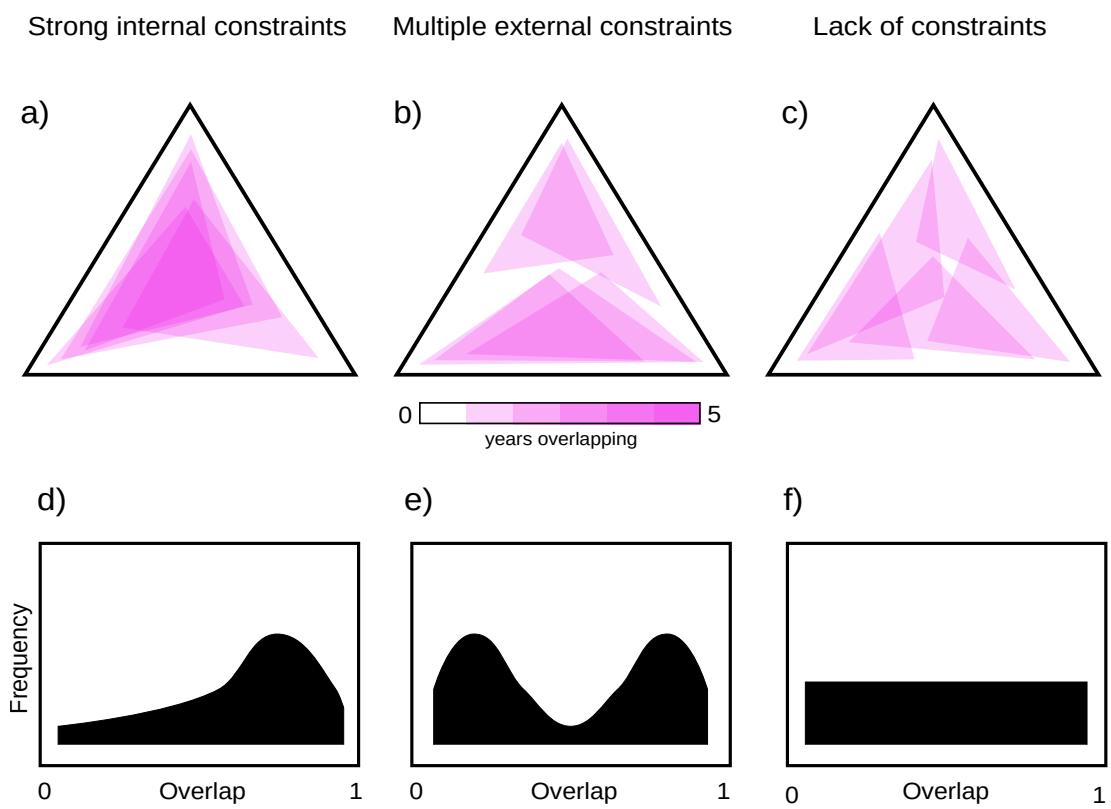
490 Figure 1. Theoretical expectations for how the feasibility domains (FDs) of a community  
491 explore the parameter space over time. (a) Strong internal constraints scenario: FDs  
492 remain concentrated in a limited region, indicating strong internal constraints. (b) Multiple  
493 external constraints scenario: FDs shift between distinct regions, suggesting multiple stable  
494 states. (c) Lack of constraints scenario: FDs spread across the entire parameter space,  
495 implying minimal constraints. (d-f) Expected distributions of overlap values between pairs  
496 of consecutive FDs for each scenario: (d) High internal constraints lead to consistently high  
497 overlap, (e) alternative stable regions result in a bimodal distribution of overlap values, and  
498 (f) no constraints produce a uniform overlap distribution.

499 Figure 2. Examples of observed feasibility domains (FDs) for selected subcommunities,  
500 each composed of three species. Each pink polygon represents the FD for a given year,  
501 illustrating the range of feasible conditions for that subcommunity. Some FDs extend  
502 beyond the triangular space, indicating scenarios where at least one species has a negative  
503 intrinsic growth rate due to facilitative effects. These regions have been cropped to display  
504 only positive intrinsic growth rates. Correspondence between species codes and scientific  
505 names can be found in Appendix S1: Table S1.

506 Figure 3. Constraints in Feasibility domains (FDs). This figure explores mean overlap  
507 between pairs of FD, calculated for subcommunities (triplets of species). Panel (a): The  
508 line plots show the accumulated mean overlap for three scenarios: (1) Observed  
509 Interactions, Observed Order (purple): Using the empirically observed matrices in their  
510 original temporal order. (2) Randomized Interactions, Observed Order (blue): Using  
511 matrices with randomized entries but maintaining the original temporal order. (3)  
512 Observed Interactions, Randomized Order (green): Using the empirically observed matrices

513 but with their temporal order randomized. Lines represent the mean calculated across all  
514 subcommunities (triplets of species), shaded areas 95% confidence intervals for each mean.  
515 Panels (b)-(d): Distribution of Pairwise Overlap. Histograms showing the distribution of  
516 the degree of overlap between all possible pairs of matrices within each scenario. Panels  
517 display the distribution of pairwise FD overlap values for each scenario: (b) Observed, (c)  
518 Randomized Matrices, (d) Disordered.

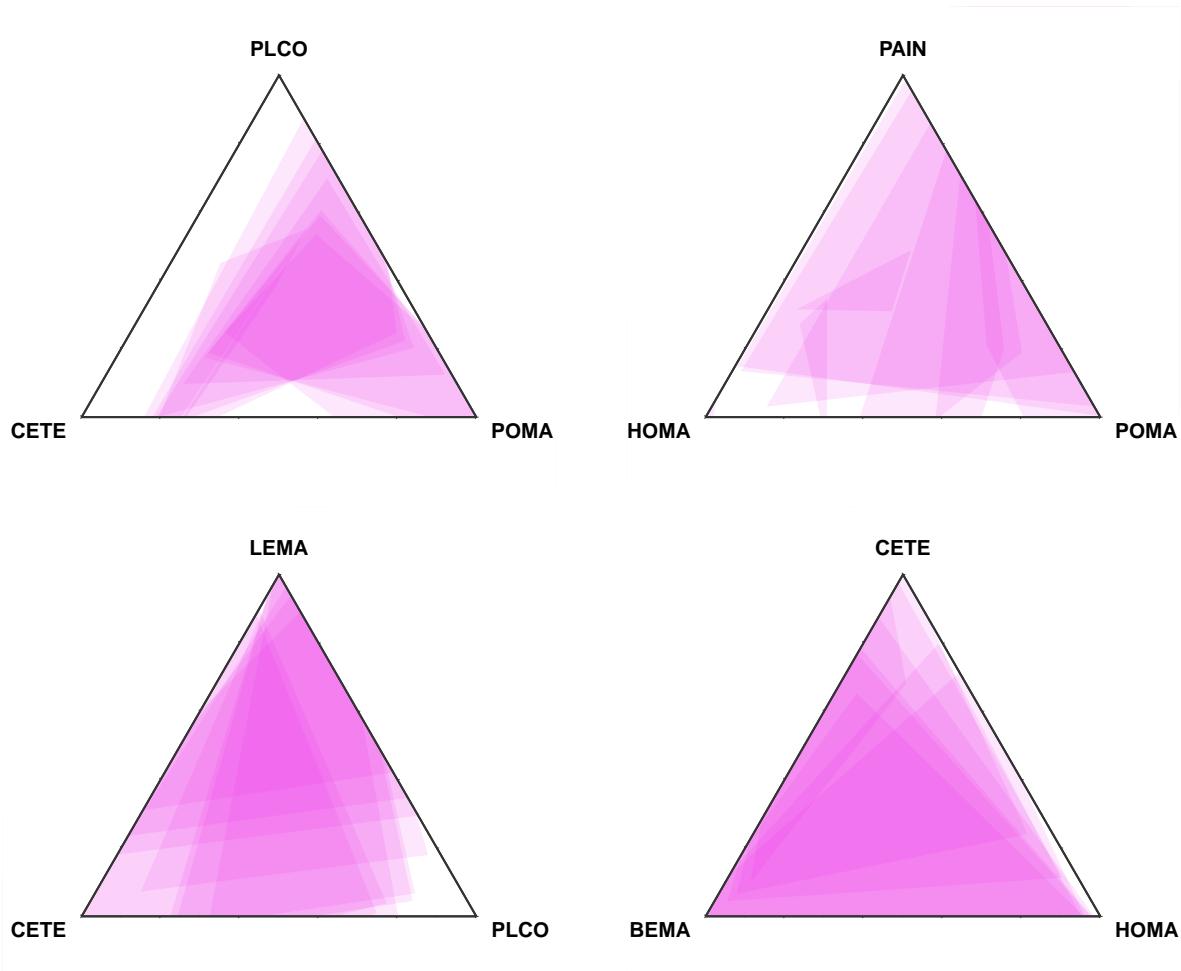
519 Figure 4. Precipitation reduces feasibility domain mean size but increases the temporal  
520 similarity of species interactions. This figure displays how annual precipitation exerts  
521 contrasting influences on two key ecological properties of subcommunities (species triplets).  
522 Panel (a) Feasibility Domain Size ( $\Omega$ ). The points denote the mean size ( $\Omega$ ) of feasibility  
523 domains, averaged across all subcommunities within a given year. Error bars represent 95%  
524 confidence intervals for these annual means. Panel (b) Interaction Matrix Similarity. The  
525 points denote the similarity between interaction matrices, quantified using the inverse of  
526 the euclidean distance between them, averaged across all subcommunities per year. Error  
527 bars represent 95% confidence intervals for these annual means. In both panels, red lines  
528 and shaded regions depict the predicted values and the 95% confidence intervals from the  
529 respective linear regressions, respectively. Also, Spearman's correlation ( $\rho$ ) is shown for  
530 each case. For illustrative purposes, we show for each panel examples of feasibility domains  
531 at the extremes of the precipitation gradient. In a), we highlight the differences in size  
532 between larger domains under drier years and smaller domains under wetter years. In b),  
533 we highlight differences in the position and shape of the feasibility domains of different  
534 subcommunities in drier years versus similar locations and shapes in wetter years.



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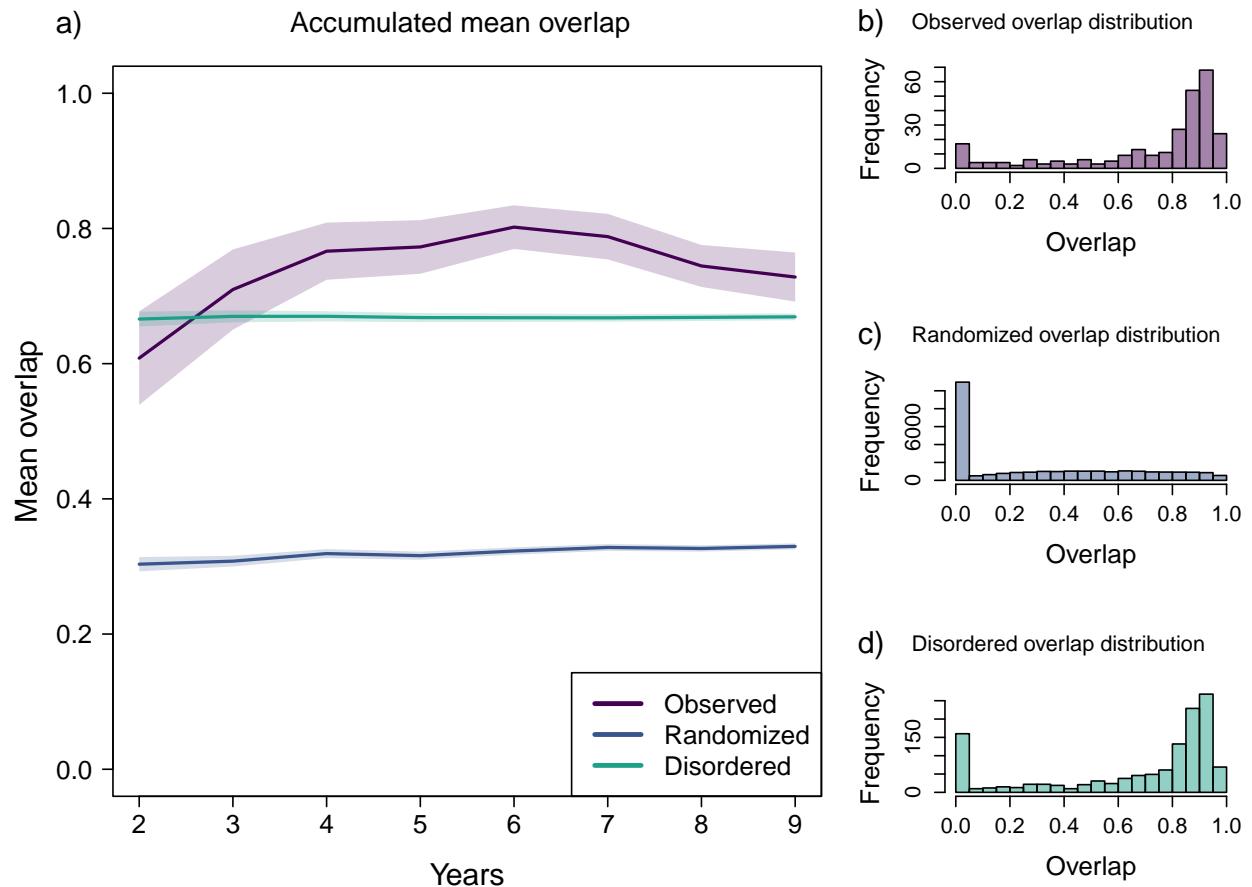
Figure 1



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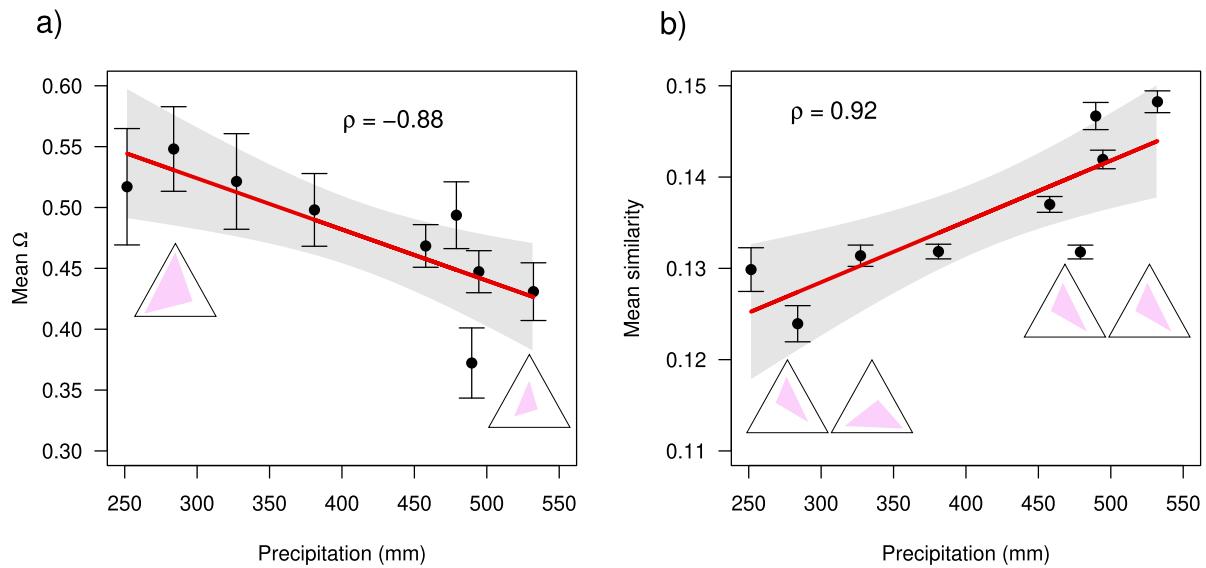
Figure 2



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Figure 3



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Figure 4

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## Appendix S1 for

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# Species interactions are internally constrained despite 549 large climatic variability

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560 **A List of species and codes**

Species	Order	Family	Abbreviation
<i>Beta macrocarpa</i>	Caryophyllales	Amaranthaceae	BEMA
<i>Centaurium tenuiflorum</i>	Gentianales	Gentianaceae	CETE
<i>Hordeum marinum</i>	Poales	Poaceae	HOMA
<i>Leontodon maroccanus</i>	Asterales	Asteraceae	LEMA
<i>Parapholis incurva</i>	Poales	Poaceae	PAIN
<i>Plantago coronopus</i>	Lamiales	Plantaginaceae	PLCO
<i>Polypogon monspeliensis</i>	Poales	Poaceae	POMA

Table S1: List of species used to estimate interactions and abbreviations used to identify them in code and plots.

561 **B Feasibility domains and overlap**

562 **B.1 Three species**

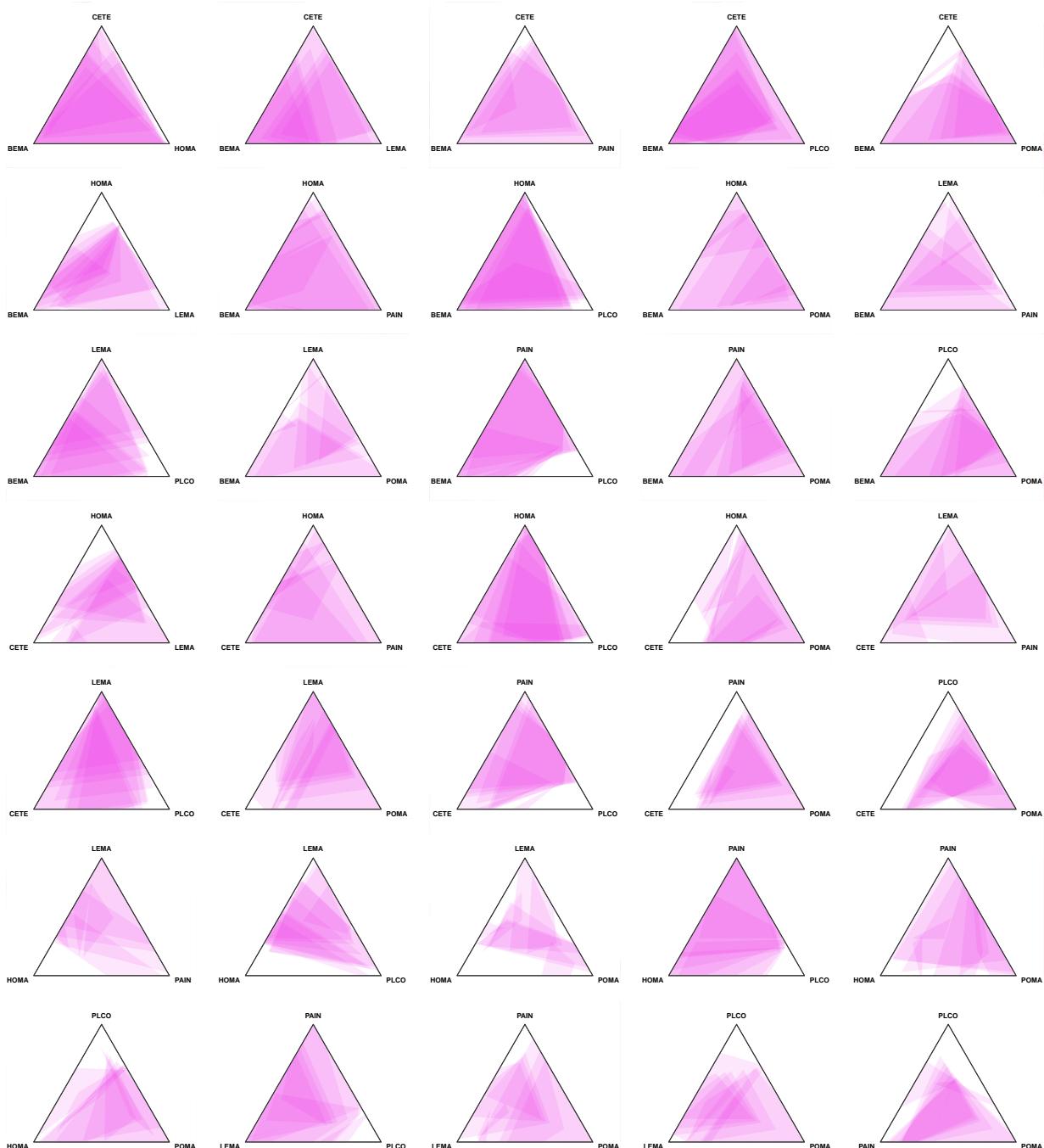


Figure S1: Feasibility domains (FDs) observed for all subcommunities (triplets of species). Each black line triangle contains the FDs observed during 9 years for a subcommunity. Each pink triangle represents the FD of one year for that subcommunity. Some FDs extend outside the triangle space (where the intrinsic growth rate for at least one species is negative) because of facilitative effects, but these regions have been cut to only show positive intrinsic growth rates. Correspondence between species codes and scientific names can be found in Appendix S3: Table S1.

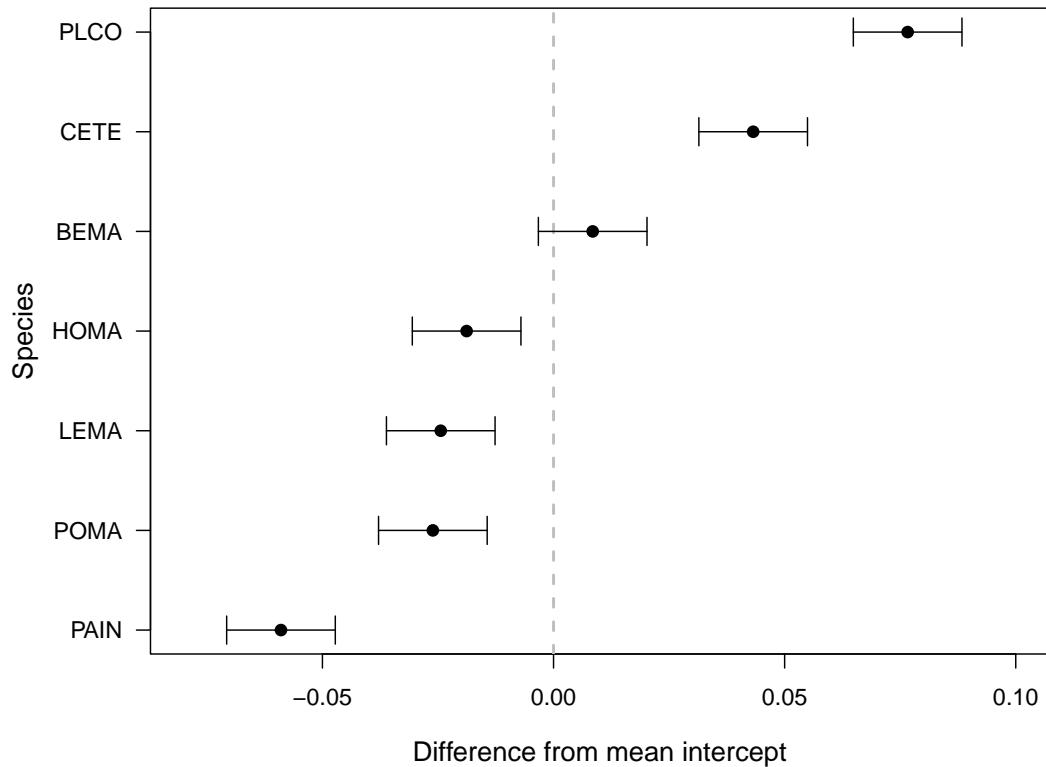


Figure S2: Species effects. Differences from the mean intercept for accumulated mean overlap caused by the presence of a species in a subcommunity (triplet of species). Estimated using a multimembership mixed model where treatment (Observed, Randomized, Disordered) and time (years) explain accumulated mean overlap, using a species-presence matrix as a random effect instead. Point estimates and 95% confidence intervals are shown.

Predictor	Estimate	Std. error	t value
Disordered (Intercept)	0.642	0.052	12.377
Observed	0.067	0.008	8.221
Randomized	-0.350	0.008	-42.712
Time (years)	0.006	0.001	3.781

Table S2: Multimembership model fixed effects. Summary table of the fixed effects estimated in the multimembership mixed model where treatment (Observed, Randomized, Disordered) and time (years) explain accumulated mean overlap, and a species-presence matrix is used as a random effect instead.

563 **B.2 Four species**

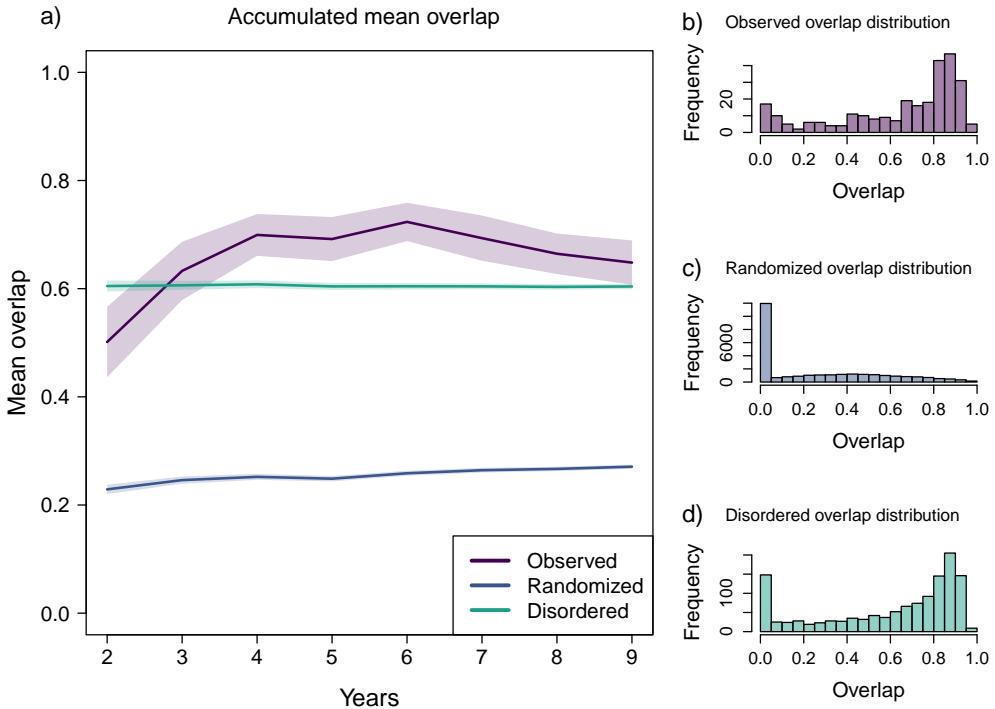


Figure S3: Constraints in Feasibility domains (FDs). This figure explores mean overlap between pairs of FD, calculated for subcommunities (groups of four of species). Panel (a): The line plots show the accumulated mean overlap for three scenarios: (1) Observed Interactions, Observed Order (purple): Using the empirically observed matrices in their original temporal order. (2) Randomized Interactions, Observed Order (blue): Using matrices with randomized entries but maintaining the original temporal order. (3) Observed Interactions, Randomized Order (green): Using the empirically observed matrices but with their temporal order randomized. Lines represent the mean calculated across all subcommunities (groups of four of species), shaded areas 95% confidence intervals for each mean. Panels (b)-(d): Distribution of Pairwise Overlap. Histograms showing the distribution of the degree of overlap between all possible pairs of matrices within each scenario. Panels display the distribution of pairwise FD overlap values for each scenario: (b) Observed, (c) Randomized Matrices, (d) Disordered.

564 **C Precipitation and precipitation effects**

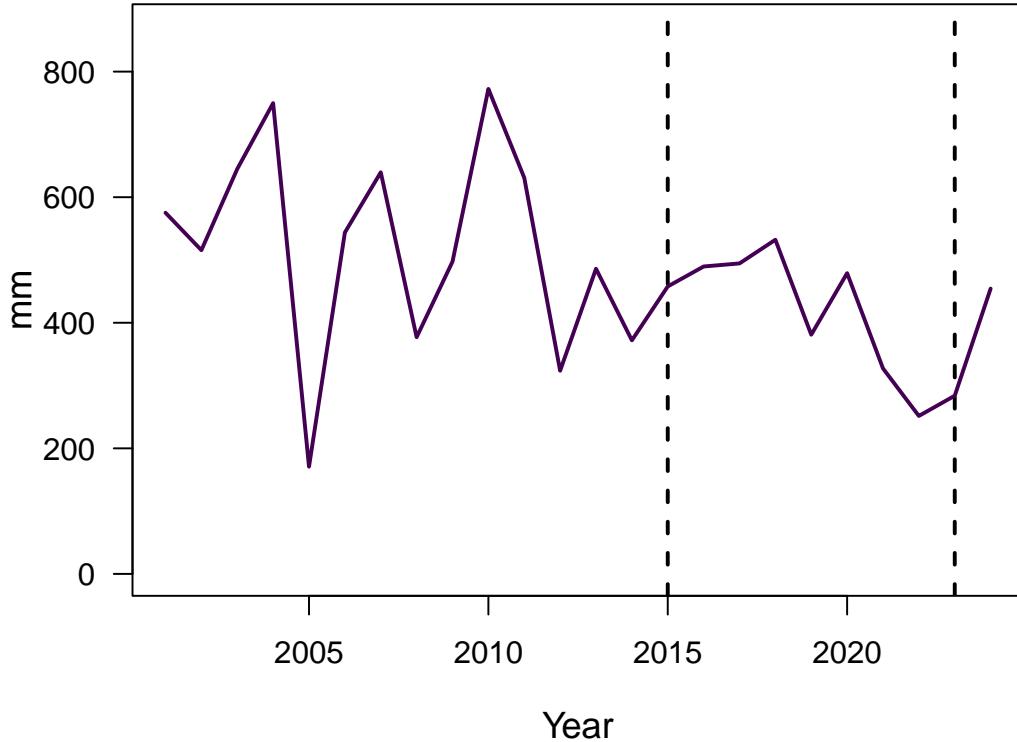


Figure S4: Precipitation time series from the study site. Precipitation data obtained from the nearest meteorological station to the study site ( $\sim 10$  km), Estación Meteorológica de Aznalcázar, Junta de Andalucía. Data is expressed as total mm of precipitation for the hydrological year (September - August). Vertical dashed bars mark the duration of the study (2015 - 2023).

Predictor	Estimate	Std. error	p-value
Intercept	0.6500	0.0508	4.1500E-06
Precipitation	-0.0004	0.0001	0.0102

Table S3: Summary table of the linear regression shown in Figure 4 a).

Predictor	Estimate	Std. error	p-value
Intercept	0.1085	7.09500E-03	1.2300E-06
Precipitation	6.6580E-05	1.6810E-05	0.0055

Table S4: Summary table of the linear regression shown in Figure 4 b).